Design and Analysis of Occupancy Studies Part 2

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Single Species; Multi-Season - Example

Single-Species Multi-Season Occupancy Studies

Analysis of Northern Spotted Owl study using unmarked

Single Species; Multi-Season - Example

Northern Spotted Owl (Strix occidentalis caurina) in California.

s=55 sites visited up to K=8 times per season between 1997 and 2001 (Y=5).

Detection probabilities relatively constant within years, but likely different among years.

1. Read in history data.

This is a $n_{sites} \times n_{years} n_{visits}$ matrix or data.frame.

All years must have the same number of visits, but just pad on the right with missing values.

```
input.history <- read.csv("NSO_pg209.csv",
header=FALSE, skip=2, na.strings="-")
input.history$V1 <- NULL # drop the site number

Nsites = nrow(input.history)
Nyears = 5
Nvisits= ncol(input.history)/Nyears</pre>
```

2. Create site level covariates (if any). These are used for initial occupancy. This is a $n_{sites} \times n_{site.covariates}$ data.frame.

- 1 site.covar <- data.frame(SiteNum=1:Nsites)</pre>
- 2 head(site.covar)

3. Create site - year level covariates (if any). These are used for colonization and extinction. This is a $n_{sites}n_{yearr} \times n_{year.site.covariates}$ data.frame. These should be in site major order as shown below.

4. Create visit level covariates (if any).

These are used for detection probabilities

This is a $n_{sites} n_{vearr} n_{visits} \times n_{visit.covariates}$ data.frame.

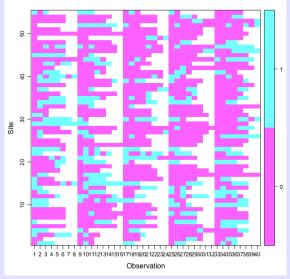
These should be in site, year, visit major order as shown below.

```
obs.covar <- data.frame(
2
       SiteNum = rep(1:Nsites, each=Nyears * Nvisits),
       Year = as.factor(rep( rep(1:Nyears, each=Nvisits),
       Visit = as.factor(rep(1:Nvisits, Nyears*Nsites)))
  > obs.covar[1:30,]
     SiteNum Year Visit
  1
  8
                      8
  9
  10
```

4. The UMF object

```
1  nso.UMF <- unmarked::unmarkedMultFrame(
2          input.history,
3          siteCovs=site.covar,
4          yearlySiteCovs=yearsite.covar,
5          obsCovs = obs.covar,
6          numPrimary=Nyears)
7  nso.UMF</pre>
```

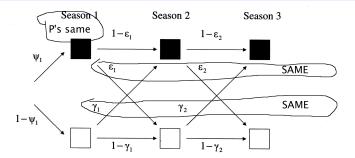
Map of detections.



Model with colonization and extinction rates parameterization. Fit the $\psi(1997), \gamma(*), \epsilon(*), p(*)$ model in the usual way.

```
mod.psiDot.gDot.eDot.pDot <- unmarked::colext(
psiformula = ~1,
gammaformula = ~ 1,
epsilonformula = ~ 1,
pformula = ~ 1,
data=nso.UMF,
se=TRUE)
summary(mod.psiDot.gDot.eDot.pDot)</pre>
```

Helpful to draw a diagram of the process model:



```
Model \psi(1997), \gamma(*), \epsilon(*), p(*) Results of model fit.
```

```
Call:
```

```
unmarked::colext(psiformula = ~1, gammaformula = ~1, epsilo
pformula = ~1, data = nso.UMF, se = TRUE)
```

AIC: 1363.32

Number of sites: 55

```
Model \psi(1997), \gamma(*), \epsilon(*), p(*) parameter estimates.
We use predict with a (new) data frame with nothing in it.
predict(mod.psiDot.gDot.eDot.pDot, type='psi')
newdata <- data.frame(dummy=1)</pre>
predict(mod.psiDot.gDot.eDot.pDot, type='psi', newdata=newd
gives:
> predict(mod.psiDot.gDot.eDot.pDot, type='psi')
   Predicted
                      SE
                             lower
                                   upper
1 0.6311598 0.06726424 0.4927218 0.7509165
2 0.6311598 0.06726424 0.4927218 0.7509165
> newdata <- data.frame(dummy=1)</pre>
> predict(mod.psiDot.gDot.eDot.pDot, type='psi', newdata=ne
  Predicted
                     SE
                            lower
                                    upper
1 0.6311598 0.06726424 0.4927218 0.7509165
```

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ parameter estimates. We use *predict* with a (new) data frame with nothing in it. predict(mod.psiDot.gDot.eDot.pDot, type='col', newdata=newdot)

- 2 3 predict(mod.psiDot.gDot.eDot.pDot, type='ext', newdata=new
- 3 predict(mod.psiDot.gDot.eDot.pDot, type='ext', newdata=new gives:
 - > predict(mod.psiDot.gDot.eDot.pDot, type='psi', newdata=not
 Predicted SE lower upper
 1 0.6311598 0.06726424 0.4927218 0.7509165
 - > predict(mod.psiDot.gDot.eDot.pDot, type='col', newdata=ne
 Predicted SE lower upper
 - 1 0.1841754 0.0427179 0.1145044 0.2827042

```
Model \psi(1997), \gamma(*), \epsilon(*), p(*) parameter estimates. We use predict with a (new) data frame with nothing in it.
```

predict(mod.psiDot.gDot.eDot.pDot, type='det', newdata=newg
gives:

```
Predicted SE lower upper 1 0.4947425 0.01858223 0.4584141 0.5311265
```

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ derived parameter estimates of occupancy in later years

There are two type of estimates

- projected for the population of ALL sites
- smoothed for the actual sites

-

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ derived parameter estimates of occupancy in later years Projected - for POPULATION of ALL sites.

What is the occupancy for the population of ALL potentia

first index = not occupied/occupied, second index=year, mod.psiDot.gDot.eDot.pDot@projected[,,1]

mod.psiDot.gDot.eDot.pDot@projected[2,,1] 5 projected(mod.psiDot.gDot.eDot.pDot) # this gives the mean

> mod.psiDot.gDot.eDot.pDot@projected[,,1] [,1] [,2] [,3] [,4][.5]

[1,] 0.3688402 0.3960537 0.4141528 0.4261901 0.4341959

[2,] 0.6311598 0.6039463 0.5858472 0.5738099 0.5658041 > mod.psiDot.gDot.eDot.pDot@projected[2,,1]

[1] 0.6311598 0.6039463 0.5858472 0.5738099 0.5658041 > projected(mod.psiDot.gDot.eDot.pDot) # this gives the mo

unoccupied 0.3688402 0.3960537 0.4141528 0.4261901 0.43419 0.6311500 0 6030463 0 5050473 0 5730000 0 56500

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ derived parameter estimates of occupancy in later years

Smoothed - for sample of actual sites

No SE are provided (but see below).

What is the actual occupancy for these particular sites

2 mod.psiDot.gDot.eDot.pDot@smoothed[2,,1:2]
3 smoothed(mod.psiDot.gDot.eDot.pDot)[2,] # this gives the m

> mod.psiDot.gDot.eDot.pDot@smoothed[2,,1:2]

[,1] [,2] [1,] 1 0.1069976 [2,] 1 0.0544300

[3,] 1 0.1538519 [4,] 1 1.0000000

[5,] 1 1.0000000
> smoothed(mod.psiDot.gDot.eDot.pDot)[2,] # this gives the

1 2 3 4 5 0.6311617 0.6084676 0.5553642 0.5756990 0.5738898

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Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ Finding growth estimates and SE using bootstrapping.

```
# Obtain standard errors for these forecasts using paramet
   psi.projected <- function(model, site) {</pre>
3
     psi.projected <- model@projected[2,,site]</pre>
4
5
     # compute population growth
     lambda <- exp(diff(log(psi.projected),1))</pre>
6
     lambda.overall <- prod(lambda) # overall growth rate over
7
8
9
     lambda.prime <- exp(diff(logit(psi.projected),1))</pre>
     lambda.prime.overall <- prod(lambda.prime) # overall grow</pre>
10
     c(psi.projected=psi.projected,
11
        lambda=
12
                       lambda,
13
       lambda.overall=lambda.overall,
       lambda.prime =lambda.prime,
14
        lambda.prime.overall=lambda.prime.overall )
15
```

psi.projected(mod.psiDot.gDot.eDot.pDot, site=1)

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ Finding growth estimates and SE using bootstrapping.

```
> psi.projected(mod.psiDot.gDot.eDot.pDot, site=1)
      psi.projected1
                           psi.projected2
                                                  psi.project
           0.6311598
                                 0.6039463
                                                        0.5858
      psi.projected4
                            psi.projected5
                                                          laml
           0.5738099
                                 0.5658041
                                                        0.9568
             lambda2
                                    lambda3
                                                          laml
           0.9700319
                                 0.9794531
                                                        0.9860
      lambda.overall
                             lambda.prime1
                                                   lambda.pr:
           0.8964514
                                 0.8911343
                                                        0.9276
       lambda.prime3
                             lambda.prime4 lambda.prime.ove
           0.9517894
                                 0.9678671
                                                        0.761
```

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ Bootstrap to obtain standard errors.

psi.projected5

lambda.overall

lambda1

lambda2 lambda3

lambda4

mod.psiDot.gDot.eDot.pDot.boot <- parboot(mod.psiDot.gDot.g</pre> cbind(est=mod.psiDot.gDot.eDot.pDot.boot@t0, 3 se=apply(mod.psiDot.gDot.eDot.pDot.boot@t.star, 2, se t(apply(mod.psiDot.gDot.eDot.pDot.boot@t.star, 2, qua 2.5% 97 est se psi.projected1 0.6311598 0.07232729 0.4999588 0.76014 psi.projected2 0.6039463 0.05104551 0.5066507 0.68279 psi.projected3 0.5858472 0.04869471 0.4959554 0.6622 psi.projected4 0.5738099 0.05355065 0.4684403 0.66400

0.5658041 0.05909911 0.4421961 0.66204

0.9568833 0.05727312 0.8403070 1.07265 0.9700319 0.04073060 0.8816002 1.04999

0.9794531 0.02893533 0.9184148 1.0353
0.9860480 0.02049825 0.9426764 1.0236

0.8964514 0.13731974 0.6408903 1.19518

0.0044040 0.44704057 0.5007005 4.44005

Fit model for p to allow for year effects, but equal within each year.

Model with colonization and extinction rates parameterization. Fit the $\psi(1997), \gamma(*), \epsilon(*), \rho(Year)$ model in the usual way.

```
mod.psiDot.gDot.eDot.pYear <- unmarked::colext(
psiformula = ~1,
gammaformula = ~ 1,
epsilonformula = ~ 1,
pformula = ~ Year,
data=nso.UMF,
se=TRUE)</pre>
```

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ Results of model fit.

AIC: 1353.528

Number of sites: 55

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ parameter estimates.

```
> predict(mod.psiDot.gDot.eDot.pYear, type='psi', newdata=
 Predicted
                 SE
                       lower
                             upper
```

- 1 0.6247288 0.06689193 0.4876139 0.7443861
- > predict(mod.psiDot.gDot.eDot.pYear, type='col', newdata= Predicted SE lower upper
- 1 0.1788409 0.04301406 0.1092631 0.2788544

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ parameter estimates.

```
> predict(mod.psiDot.gDot.eDot.pYear, type='ext', newdata='
Predicted SE lower upper
1 0.1423004 0.03280271 0.08922963 0.2193345
```

- > newdata <- data.frame(Year=as.factor(1:5))</pre>
- > predict(mod.psiDot.gDot.eDot.pYear, type='det', newdata='
 Predicted SE lower upper
- 1 0.5905707 0.03942752 0.5116810 0.6650582
- 2 0.5224669 0.04047178 0.4432440 0.6005754
- 3 0.4074948 0.04418033 0.3245423 0.4960781
- 4 0.3848536 0.04125135 0.3077810 0.4681730
- 5 0.5365865 0.03916093 0.4595733 0.6118931...

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ Projected estimates of occupancy for POPULATION and SAMPLE

> mod.psiDot.gDot.eDot.pYear@projected[2,,1]

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$

lambda1

lambda2

lambda3

lambda4

lambda.overall

lambda.prime1

lambda.prime2 lambda.prime3

lambda.prime4

Growth parameters and standard errors via bootstrapping

est se psi.projected1 0.6247288 0.06587862 0.4894743 0.75166

psi.projected2 0.6029434 0.04868917 0.5191508 0.70289

0.5881543 0.04948117 0.4887079 0.69198 psi.projected3

psi.projected4 0.5781145 0.05623694 0.4684003 0.68989

psi.projected5 0.5712989 0.06307565 0.4525634 0.69206 0.9651283 0.05627099 0.8765583 1.09893

0.9829301 0.02849954 0.9276229 1.04286

0.9754717 0.03969023 0.9061482 1.0669

lambda prime overall 0 8005023 0 33738711 0 4114786 1 $\frac{9708}{1}$

0.9121745 0.14214467 0.6666104 1.23989

0.9404430 0.09579496 0.7879826 1.16964

0.9595389 0.06676223 0.8497704 1.11509

0.9724999 0.04760985 0.8932224 1.07850

0.9882107 0.02072323 0.9395945 1.02749

0.9144751 0.13799503 0.7035495 1.2690

2.5%

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Fit the $\psi(1997)$, p(year), $\epsilon(year)$, $\gamma(year)$ model.

Model with colonization and extinction rates parameterization. Fit the $\psi(1997)$, p(year), $\epsilon(year)$, $\gamma(year)$ model.

```
mod.psiDot.gYear.eYear.pYear <- unmarked::colext(
psiformula = ~1,
gammaformula = ~ Year,
epsilonformula = ~ Year,
pformula = ~ Year,
data=nso.UMF,
se=TRUE)</pre>
```

What model would represent NO CHANGE IN OCCUPANCY in individual sites over the multiple seasons?

What model would represent NO CHANGE IN OCCUPANCY in individual sites over the multiple seasons, i.e. convert this to an 'equivalent single season model=?

 $\gamma_y = 0$ and $\epsilon_y = 0$ for all years.

Fit the model and FIX some parameters **Not possible in unmarked**.

Here is the current AIC table:

	nPars	AIC	delta	AICwt	cur
mod.psiDot.gDot.eDot.pYear	8	1353.53	0.00	0.7385	
<pre>mod.psiDot.gYear.eYear.pYear</pre>	14	1355.65	2.12	0.2560	
mod.psiDot.gDot.eDot.pDot	4	1363.32	9.79	0.0055	

What do you conclude?

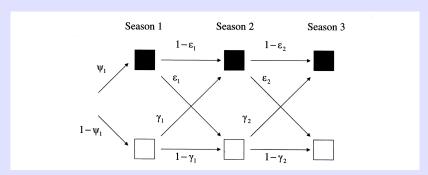
Model averaging only works for internal parameters and not derived parameters (groan), but you could write your own model averaging routine (double groan).

What model would represent RANDOM occupancy over seasons, i.e. no site fidelity between seasons?

A RANDOM occupancy model says that occupancy in each season is a random process with no regard to sites being occupied or not occupied in previous seasons. For example, migrating birds return each year to select nesting sites but the process each year is independent of previous years. Site could be occupied for multiple years in a row, but this the result of random chance rather than any site fidelty.

A RANDOM occupancy model implies that an occupied site in season y has the same chance of being occupied in year y+1 (i.e. $(1-\epsilon_y)$) as does an unoccupied site in season y being occupied in year y+1 (i.e. γ_y).

Or ... RANDOM occupancy $\rightarrow \gamma_y = (1 - \epsilon_y)$.



```
Model: \psi(1997), p(year), \epsilon(year), \gamma = 1 - \epsilon
This is equivalent to Model: \psi(year), p(year) where \gamma = 1 - \epsilon is enforced internally).
```

Currently not available in the <code>colext()</code> but you can "fake it" by analyzing each year separately using a single season occupancy model. But then you can't easily find growth rates and their standard errors. See https://groups.google.com/forum/#!searchin/unmarked/random\$20occupancy%7Csort:date/unmarked/-TINYk51EHs/Au5pyyW0BQAJ

Single Species; Multi-Season - NSO - unmarked

What model would represent a population in equilibrium in occupancy?

Single Species; Multi-Season - NSO - unmarked

What model would represent a population in equilibrium in occupancy? $\psi_{y+1}=\psi_y\to\psi_{EQ}=\tfrac{\gamma}{\gamma+\epsilon}$

Not possible in unmarked.

Single Species; Multi-Season - NSO - unmarked

Conclusion:

- Changed in occupancy best represented by a Markov process (as expected), i.e. site fidelity at the species level (but not necessarily at the individual level).
- Random occupancy or no changes in occupancy have no support.
- Highest weight given to models in equilibrium (90% of model weights). (not possible in unmarked)

unmarked mostly is adequate.

- Derived estimates don't include population growth.
- Random occupancy models not directly implemented.

Single Species; Multi-Season - Example

Single-Species Multi-Season Occupancy Studies

Analysis of Northern Spotted Owl study using JAGS.

Using JAGS:

- NOT FOR THE FAINT OF HEART!
- Order of various covariate matrices IMPORTANT see code for details
- Use *model.matrix()* to generate the design matrices.
 - You need to understand the underlying parameterization and how to interpret
- Huge amounts of output that you must SELECTIVELY view in an efficient manner.

Northern Spotted Owl (Strix occidentalis caurina) in California.

s=55 sites visited up to K=8 times per season between 1997 and 2001 (Y=5).

Detection probabilities relatively constant within years, but likely different among years.

Read in data and create the covariate matrices.

- History is $n_{sites} \times n_{years} n_{visits}$ matrix. Number of visits must be consistent among years, but just pad on the right.
- Site covariates is $n_{sites} \times n_{covariates}$ Use categorical variables when every possible rather than creating indicator variables.
- Site-Year covariates is n_{sites} n_{years} × n_{covariates} in Year major order, i.e. stack columns of yearly values. Will automatically add site covariates to the matrix.
- Visit covariates is n_{sites} n_{years} n_{visits} × n_{covariates} in Year/Visit/Site major order, i.e. stack columns of site covariates for each visit. Site-Year covariates automatically added.

Create your design matrices using *model.matrix()*

9 # Create design matrix for local colonization rate using y
10 covar.gamma <- cbind(yearsite.covar[,c("Site","Year")],
11 model.matrix(~as.factor(Year), data=yearsite.covar))
12

Create design matrix for detection probabilities
covar.p <- cbind(Site, Year,
model.matrix(~as.factor(Year), data=obs.covar)</pre>

Common error is use *Year* as a continuous variable rather than a factor. Notice use of different covariate matrices. All covariate models operate on *logit()* of the parameter.

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No missing values allowed in site or site-year covariates. Histories (and covariate rows) with missing visit information automatically deleted.

```
# Remove rows corresponding to missing values in all input
no.visit <- is.na(History)

Site <- Site [!no.visit]
Year <- Year [!no.visit]
Visit <- Visit [!no.visit]
History<- History[!no.visit]
covar.p<- covar.p[!no.visit,]</pre>
```

```
Model \psi(1997), \gamma(*), \epsilon(*), p(*) parameter estimates.
```

mean sd psi[1,1] 0.6323608 0.06696484

```
Model \psi(1997), \gamma(*), \epsilon(*), p(*) parameter estimates.
```

```
> # Estimate of local colonization probability for each us
mean sd
gamma[1,1] 0.1833509 0.04244442
```

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ derived parameter estimates of occupancy in later years

	mean	sd
psi[1,1]	0.6323608	0.06696484
psi[1,2]	0.6051648	0.05117052
psi[1,3]	0.5870344	0.05117800
psi[1,4]	0.5748694	0.05612736
psi[1,5]	0.5666558	0.06118645

Model $\psi(1997), \gamma(*), \epsilon(*), p(*)$ derived parameter estimates of population growth.

```
meansdlambda[1,1]0.96046600.05289506lambda[1,2]0.97051840.03689389lambda[1,3]0.97865150.02604304lambda[1,4]0.98480330.01849410lambda.prime[1,1]0.89546180.13505411lambda.prime[1,2]0.93062570.08751699lambda.prime[1,3]0.95313460.05863444lambda.prime[1,4]0.96807480.04006228
```

SE are trivial to find using Bayesian methods

Fit model for p to allow for year effects, but equal within each year.

Model with colonization and extinction rates parameterization. Fit the $\psi(1997), \gamma(*), \epsilon(*), p(Year)$ model in the usual way.

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ parameter estimates.

> # Estimate of local colonization probability for each up mean sd gamma[1,1] 0.1779443 0.04172938

```
Model \psi(1997), \gamma(*), \epsilon(*), p(YEAR) parameter estimates.
```

```
> # Estimate of local extinction probability for each unimean sd
epsilon[1,1] 0.1407420 0.03207532
```

. . .

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ derived parameter estimates of occupancy in later years

> # Derived parameters - estimated occupancy for each unit

mean sd

psi[1.1] 0.6261110 0.06576700

psi[1,1]	0.6261110	0.06576700
psi[1,2]	0.6046207	0.05023741
psi[1,3]	0.5899712	0.04990449
psi[1,4]	0.5799238	0.05476636
psi[1,5]	0.5729918	0.05995964

Model $\psi(1997), \gamma(*), \epsilon(*), p(YEAR)$ derived parameter estimates of population growth

```
meansdlambda[1,1]0.96912500.05157563lambda[1,2]0.97632840.03630422lambda[1,3]0.98242160.02589554lambda[1,4]0.98718260.01860532lambda.prime[1,1]0.91753140.13137925lambda.prime[1,2]0.94414820.08693480lambda.prime[1,3]0.96150560.05926650lambda.prime[1,4]0.97323890.04113874
```

Fit the $\psi(1997)$, p(year), $\epsilon(year)$, $\gamma(year)$ model.

What model would represent NO CHANGE IN OCCUPANCY in individual sites over the multiple seasons?

What model would represent NO CHANGE IN OCCUPANCY in individual sites over the multiple seasons, i.e. convert this to an 'equivalent single season model=?

 $\gamma_y = 0$ and $\epsilon_y = 0$ for all years.

You would specify HIGHLY informative priors that the $\beta_{epsilon} = 0$.

Very complex to do model comparison and model averaging in Bayesian methods for mere mortals.

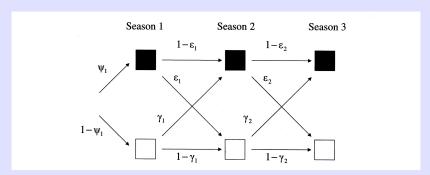
See me for details.

What model would represent RANDOM occupancy over seasons, i.e. no site fidelity between seasons?

A RANDOM occupancy model says that occupancy in each season is a random process with no regard to sites being occupied or not occupied in previous seasons. For example, migrating birds return each year to select nesting sites but the process each year is independent of previous years. Site could be occupied for multiple years in a row, but this the result of random chance rather than any site fidelty.

A RANDOM occupancy model implies that an occupied site in season y has the same chance of being occupied in year y+1 (i.e. $(1-\epsilon_y)$ as does an unoccupied site in season y being occupied in year y+1 (i.e. γ_y).

Or ... RANDOM occupancy $\rightarrow \gamma_y = (1 - \epsilon_y)$.



A RANDOM occupancy model is fit using type=do.4. Now the parameters are ψ (now for each season), and p with $\gamma=1-\epsilon$ enforced internally depending on estimates of ψ for each year.

Not currently implemented in *JAGS*, but see me if you are interested (not difficult).

You can always fit a SSMS model like in unmarked.

What model would represent a population in equilibrium in occupancy?

What model would represent a population in equilibrium in occupancy? $\psi_{y+1}=\psi_y\to\psi_{EQ}=\tfrac{\gamma}{\gamma+\epsilon}$

Not currently implemented in JAGS.

Conclusion:

- Bayesian methods make it easy to find posterior beliefs, e.g. what is Pr(trend ¿0).
- Very flexible but requires discipline to implement and debug
 (!)
- Model selection and averaging not for mere mortals.
- Model assessment (goodness of fit) possible but not implemented here.

Single Species; Multi-season - Covariates - unmarked

The second and third parameterizations of *PRESENCE* and *MARK* are not available in *unmarked*.

Random occupancy model not available directly in *unmarked*, but refer to web link in previous slides for work around.

Single Species; Multi-season - Covariates - JAGS

The second and third parameterizations of *PRESENCE* and *MARK* are not available in *JAGS* but are readily implemented (see me for details).

Random occupancy model not available directly in *JAGS*, but contact me for details on work around.